## Tennessee Comprehensive Assessment Program <br> 

## Algebra II

 Practice Test

Please PRINT all information in the box.

Student Name: $\qquad$

Teacher Name: $\qquad$

School: $\qquad$

District: $\qquad$ practice test may contain item types that no longer appear on the operational assessment.


Published under contract with the Tennessee Department of Education by Educational Testing Service (ETS), Princeton, NJ 08541 . Copyright © 2019 by Tennessee Department of Education. All rights reserved. No part of this publication may be copied, reproduced, or distributed in any form or by any means, or stored in a database or retrieval system, without the prior express written consent of the Tennessee Department of Education.

## TNReady Math Reference Sheet-High School

1 inch $=2.54$ centimeters
1 mile $=5,280$ feet
1 mile $=1,760$ yards
1 mile $=1.609$ kilometers
1 kilometer $=0.62$ mile
1 meter $=39.37$ inches

1 pound = 16 ounces
1 pound $=0.454$ kilograms
1 kilogram $=2.2$ pounds
1 ton $=2,000$ pounds

1 cup $=8$ fluid ounces
1 pint $=2$ cups
1 quart $=2$ pints
1 gallon $=4$ quarts
1 gallon $=3.785$ liters
1 liter $=0.264$ gallons
1 liter = 1,000 cubic centimeters

Exponential Growth: $y=a(1+r)^{t}$

Exponential Decay: $y=a(1-r)^{t}$

Compound Interest: $A=P\left(1+\frac{r}{n}\right)^{n t}$
Continually Compounding Interest:
$A=P e^{r t}$

Arithmetic Sequence: $a_{n}=a_{1}+(n-1) d$

Geometric Sequence: $a_{n}=a_{1}(r)^{n-1}$
Finite Geometric Series: $S_{n}=\frac{a_{1}\left(1-r^{n}\right)}{1-r}$

Degrees: 1 degree $=\frac{\pi}{180}$ radians

Radians: 1 radian $=\frac{180}{\pi}$ degrees

## No test material on this page

## Directions

This test has Subpart 1, Subpart 2, and Subpart 3. Each subpart contains various types of assessment questions.

You MAY NOT use a calculator in Subpart 1 of this test.

## Sample: Multiple choice (one correct response)

Which expression is equivalent to $\frac{x^{2}+2 x-24}{3 x+18}$ ?
A. $\frac{x-4}{3}$
B. $\frac{x+6}{3 x+6}$
c. $\frac{x-4}{x+6}$
D. $\frac{x^{2}+2 x-4}{3 x^{2}+3}$

1 Simplify the expression $(2-3 i)(4+2 i)$.
A. 14
B. $6 i$
C. $2-8 i$
D. $14-8 i$

2 Fannie is making a rectangular blanket. The length of the blanket is 10 inches greater than its width, $w$, in inches.

Write the function, $f(w)$, that describes the area, in square inches, of Fannie's blanket as a function of the width, $w$.

Enter your answer in the space provided.
$\square$

3 What is the remainder when $f(x)=x^{3}+3 x^{2}-10 x-14$ is divided by $(x-3)$ ? Enter your answer in the space provided.

4 Which expression is equivalent to $(4 x+6 y)^{2}$ ?
M. $16 x^{2}+36 y^{2}$
P. $4 x^{2}+2(4 x)(6 y)+6 y^{2}$
R. $(4 x)^{2}+2(4 x)(6 y)+(6 y)^{2}$
S. $(4 x)^{2}+(4 x)(6 y)+(6 y)^{2}$

5 Which expression is the correct factorization of $x^{6}-y^{6}$ ?
A. $(x+y)^{3}(x-y)^{3}$
B. $\left(x^{2}-y^{2}\right)\left(x^{4}+2 x y+y^{4}\right)$
C. $(x-y)(x+y)\left(x^{2}+x y+y^{2}\right)\left(x^{2}-x y+y^{2}\right)$
D. $(x-y)\left(x^{2}+2 x y+y^{2}\right)(x+y)\left(x^{2}-2 x y+y^{2}\right)$

6 What value of $x$ makes the equation $\frac{3}{x+3}=\frac{9}{x^{2}-9}$ true?
Enter your answer in the space provided.
$\square$

7 Jamie deposits $\$ 627$ into a savings account. The account has an interest rate of $3.5 \%$, compounded quarterly.

Write the function that gives the amount of money in dollars, $J(t)$, in Jamie's account $t$ years after the initial deposit.

Enter your answer in the space provided.
$\square$

8 Which expression is equivalent to $\sqrt{16 a^{4} x^{6}}$, when $a>0$ and $x>0$ ?
M. $4 a^{2} x^{3}$
P. $4 a^{2} x^{4}$
R. $8 a^{2} x^{3}$
S. $8 a^{2} x^{4}$

9 The formula to determine the pH of a solution, given its hydronium ion concentration, is $y=-\log (x)$.

- $x$ represents the hydronium concentration
- $y$ represents the pH of the solution

What equation represents the hydronium ion concentration in terms of the pH ?
A. $x=(-10)^{y}$
B. $x=-10^{y}$
C. $x=(-10)^{-y}$
D. $x=10^{-y}$

## No test material on this page

## Directions

Subpart 2 of this test contains various types of assessment questions.

You MAY use a calculator in Subpart 2 of this test.


Do not go on to the next page until told to do so.

10 The 4th term of a sequence is 108 . Each term after the first is three times the previous term.

Write an explicit function that models the general term of the sequence $f(n)$.
Enter your answer in the space provided.
$\square$

11 What is one solution to $3 x^{2}+4 x+8=0$ ?
Enter your answer in the space provided.
$\square$

12 A system of equations is shown.

$$
\begin{aligned}
& f(x)=-x^{2}+6 x-4 \\
& g(x)=|x-3|-1
\end{aligned}
$$

What is the greatest value of $x$ for which $f(x)=g(x)$ ?
Enter your answer in the space provided.
$\square$

## 13 Part A

A person's batting average is determined by dividing the number of hits by the number of at bats. William has 11 hits in 53 at bats and has a batting average of 0.208 . He wants to have a batting average of at least 0.300 .

Which equation could be used to determine $x$, the number of hits in a row William needs to get in order to have a batting average of at least 0.300 ?
A. $0.300 \leq \frac{11 x}{53 x}$
B. $0.300 x \leq \frac{11}{53}$
C. $0.300 \leq \frac{11+x}{53}$
D. $0.300 \leq \frac{11+x}{53+x}$

## Part B

How many hits in a row after his first 53 times at bat would William have to hit in order to have a batting average of exactly 0.300 ?

Enter your answer in the space provided.
$\square$

14 What is $\sin \theta$ if $\theta$ is an angle in the third quadrant and $\tan \theta=1$ ?
M. $\frac{\sqrt{2}}{2}$
P. $-\frac{\sqrt{2}}{2}$
R. $\frac{1}{2}$
S. $-\frac{1}{2}$
15. A researcher wants to determine if the behavior of children is affected by playing video games that have violent content. He asks the parents of 100 children in a day care center how often each child plays video games and whether the video games they play have violent content. The children are then allowed to play in a controlled environment, such as the day care center's playground. Any violent behaviors are then noted.

What type of study is the researcher conducting?
A. census
B. experiment
C. observational study
D. sample survey

16 The function $f(x)$ is given by the equation $f(x)=3\left(x^{2}+2\right)$. The values for the quadratic function $h(x)$ are shown in the table.

| $\boldsymbol{x}$ | -2 | -1 | 0 | 1 | 2 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{h}(\boldsymbol{x})$ | 6 | -3 | -6 | -3 | 6 |

Which statement about the $y$-intercept of $f(x)$ is true?
M. It is 12 units above the $y$-intercept of $h(x)$.
$\mathbf{P}$. It is 8 units above the $y$-intercept of $h(x)$.
R. It is 6 units above the $y$-intercept of $h(x)$.
S. It is 4 units above the $y$-intercept of $h(x)$.

17 A survey asked 410 students whether they would eat food served in the school cafeteria. The results are recorded in the table shown.

| Grade | Yes | No |
| :---: | :---: | :---: |
| 9th | 67 | 33 |
| 10th | 63 | 47 |
| 11th | 32 | 68 |
| 12th | 12 | 88 |

What is the probability that a student will not eat food served in the school cafeteria, given that the student is in 10th grade?

Enter your answer, rounded to the nearest hundredth, in the space provided.
$\square$

18 A rock is dropped from a hot air balloon at a height of 100 meters. The rock's height from the ground in meters, $h(t)$, is modeled by the formula $h(t)=-4.9 t^{2}+100$, where $t$ is the time in seconds.

What is the average rate of change in $\mathrm{m} / \mathrm{s}$ of the height of the rock between 2 and 4 seconds?
A. -4.9
B. -9.8
C. -29.4
D. -58.8

This is the end of Subpart 2 of the Algebra II Test. Do not go on to the next page until told to do so.

## No test material on this page

## No test material on this page

## Directions

Subpart 3 of this test contains various types of assessment questions.

You MAY use a calculator in Subpart 3 of this test.


Do not go on to the next page until told to do so.

19 Is $(x+2)$ a factor of $x^{3}-x^{2}-x-2$ ?
A. Yes, the remainder is -12 .
B. No, the remainder is 0 .
C. No, the remainder is -12 .
D. Yes, the remainder is 0 .

20 The graph shows the exponential growth of the number of organisms in a Petri dish over a 12-hour period.

| Time <br> (hours) | Number of <br> Organisms |
| :---: | :---: |
| 0 | 25 |
| 2 | 36 |
| 4 | 52 |
| 6 | 68 |
| 8 | 88 |
| 10 | 104 |
| 12 | 151 |



To the nearest whole organism, how many organisms are expected to be in the Petri dish at 15 hours?

Enter your answer in the space provided.
$\square$

21 Calvin purchases a piece of heavy machinery for $\$ 32,300$. The value of the machine depreciates at an annual rate of $8.3 \%$.

Which function represents the value of the machine with an approximate equivalent monthly depreciation rate?
M. $f(t)=32,300\left(0.917^{\frac{1}{12}}\right)^{t}$
P. $f(t)=32,300\left(1.083^{\frac{1}{12}}\right)^{t}$
R. $f(t)=32,300\left(0.917^{\frac{1}{12}}\right)^{12 t}$
S. $f(t)=32,300\left(1.083^{\frac{1}{12}}\right)^{12 t}$

22 Two students work the same problem:

| Jamie: | Taylor: |
| :---: | :---: |
| $\frac{1}{x+3}=\frac{5}{2 x+5}$ | $\frac{1}{x+3}=\frac{5}{2 x+5}$ |
| Step 1: $\frac{1}{x+3}=\frac{1}{2 x+1}$ | Step 1: $2 x+5=5 x+15$ |
| Step 2: $2 x+1=x+3$ | Step 2: 5-15-5x-2x |
| Step 3: $2 x-x=3-1$ | Step 3: $-10=3 x$ |
| Step 4: $\quad x=2$ | Step 4: $\frac{-10}{3}=x$ |

Which statement is true?
A. Jamie is right, because the 5 in the numerator and the 5 in the denominator will simplify to 1 .
B. Taylor is right, because $1(2 x+5)=5(x+3)$ is one method to solve a proportion.
C. Jamie is wrong, because from step 2 to step 3 she should have added $x$ to both sides.
D. Taylor is wrong, because from step 3 to step 4 he should have divided both sides by -10 .

23 The graph of a system of equations is shown.


What is the $x$-coordinate of one of the solutions to the system of equations?
Enter your answer in the space provided.
$\square$

24 A chemical is added to water to a concentration of 15 parts per million ( ppm ). Readings are taken every one half hour to see how much of the chemical remains. The readings are recorded in the table shown.

| Time, $\boldsymbol{t}$ <br> (hours) | 0.0 | 0.5 | 1.0 | 1.5 | 2.0 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Concentration, $\boldsymbol{C}$ <br> (ppm) | 15.0 | 13.4 | 12.0 | 10.7 | 9.6 |

Which function models the concentration of the chemical in $t$ hours?
M. $C(t)=0.3143(14.99)^{t}$
P. $C(t)=14.99(0.3143)^{t}$
R. $C(t)=14.99(0.7997)^{t}$
S. $C(t)=0.7997(14.99)^{t}$

25 Select each function that has an inverse that is also a function for all values of $x$.
A. $f(x)=2 x^{2}+4 x-3$
B. $f(x)=2 x+3$
C. $f(x)=\frac{3}{2} x+2$
D. $f(x)=2 x^{3}+2$
E. $f(x)=2 x^{4}+3 x^{2}-x+1$

26 What value of $t$, to the nearest hundredth, makes the equation $4(10)^{3 t}=12$ true? Enter your answer in the space provided.
$\square$

This is the end of the test.

## Answer Document

Name: $\qquad$

Subpart 1 Practice Test Questions

1. (A) (B) (C) (D)
2. 


3.

4. (ㄴ) © ®
5. (A) (B) (C) (D)
6.

7.

8. © © ® ® ( ${ }^{(1)}$
9. (A) (B) (C) (D)

## Subpart 2 Practice Test Questions

10. 


11.

12.

13. Part A: (A) (B) (C)

14. (1) © ® (ㄷ
15. (A) (B) (C) (ㅁ)
16. (ㄷ) © ® ® (ㄷ
17.

18. (A) (B) (C) (D)

## Subpart 3 Practice Test Questions

19. (A)
(B) ©
(D)
20. 


21. (®) © ® ® (s)
22. (A) (B) (C) (D)
23. $\square$
24. (1) ® ® ® (s)
25. (A) (B) © () (E) (Select all that apply)
26.


## No test material on this page

## Subpart 1 Practice Test Questions

1. (A) (B) (C)
2. 

$$
f(w)=w(w+10) \text { or equivalent }
$$

3. $\square$
4. (I) ©
(5)
5. (A) (B)
(
6. 

6
7.

$$
J(t)=627(1.00875)^{4 t} \text { or equivalent }
$$

8. $\square^{\circledR}$ ®
9. (A) (B) (C)

## Subpart 2 Practice Test Questions

10. 

$$
f(n)=4\left(3^{n-1}\right)
$$

11. 

$$
\frac{-2+2 i \sqrt{5}}{3} \text { or } \frac{-2-2 i \sqrt{5}}{3} \text { or equivalent }
$$

12. $\square$
13. Part A: (A) (B) (C)

14. (1) ® (ㄷ
15. (A)
(B)
(D)
16. 
17. 


18. (A) (B) ()

## Subpart 3 Practice Test Questions

19. 

(A)
(B)
(D)
20.

Accept any answer from 219 to 233
21. (ㄷ) © $\bigcirc$ (ㄷ
22. (A) (C) (D)
23. $\square$
24. (ㄷ) © $\bigcirc$ (ㄷ
25. © (A) (E) (Select all that apply)
26. $\square$

## No test material on this page

| TNReady Practice Test Standards Alignment and Key - Algebra II |  |  |
| :---: | :---: | :---: |
| Subpart 1 | Key | Standard |
| 1 | D | A2.N.CN.A. 2 |
| 2 | $f(w)=w(w+10)$ | A2.F.BF.A. 1 |
| 3 | 10 or 10/(x-3) | A2.A.APR.A. 1 |
| 4 | R | A2.A.SSE.A. 1 |
| 5 | C | A2.A.SSE.A. 1 |
| 6 | 6 | A2.A.REI.A. 2 |
| 7 | $J(t)=627(1.00875)^{4 t}$ or equivalent | A2.F.LE.A. 1 |
| 8 | M | A2.N.RN.A. 2 |
| 9 | D | A2.A.CED.A. 2 |
| Subpart 2 |  |  |
| 10 | $f(n)=4\left(3^{n-1}\right)$ | A2.F.BF.A. 2 |
| 11 | $\frac{-2+2 i \sqrt{5}}{3} \text { or } \frac{-2-2 i \sqrt{5}}{3}$ | A2.N.CN.B. 3 |
| 12 | 5 | A2.A.REI.D. 6 |
| 13 | Part A: D Part B: 7 | A2.A.CED.A. 1 |
| 14 | P | A2.F.TF.B.3b |
| 15 | C | A2.S.IC.A. 1 |
| 16 | M | A2.F.IF.B. 5 |
| 17 | 0.43 | A2.S.CP.A. 3 |
| 18 | C | A2.F.IF.A. 2 |
| Subpart 3 |  |  |
| 19 | C | A2.A.ARP.A. 1 |
| 20 | Accept any answer from 219 to 233 | A2.S.ID.B.2a |
| 21 | R | A2.A.SSE.B.2a |
| 22 | B | A2.A.REI.A. 1 |
| 23 | 0 or 2 | A2.A.REI.C. 5 |
| 24 | R | A2.A.SSE.B. 2 |
| 25 | B, C, D | A2.F.BF.B. 4 |
| 26 | 0.16 | A2.F.LE.A. 2 |

## No test material on this page

Tennessee Comprehensive Assessment Program TCAP Algebra II
Practice Test


